Intraseasonal and Seasonally Persisting Patterns of Indian Monsoon Rainfall

V. KRISHNAMURTHY AND J. SHUKLA

Center for Ocean–Land–Atmosphere Studies, Institute of Global Environment and Society, Inc., Calverton, Maryland, and School of Computational Sciences, George Mason University, Fairfax, Virginia

(Manuscript received 13 June 2005, in final form 20 April 2006)

ABSTRACT

The space–time structure of the active and break periods of the Indian monsoon has been studied using 70-yr-long high-resolution gridded daily rainfall data over India. The analysis of lagged composites of rainfall anomalies based on an objective categorization of active and break phases shows that the active (break) cycle, with an average life of 16 days, starts with positive (negative) rainfall anomalies over the Western Ghats and eastern part of central India and intensifies and expands to a region covering central India and parts of north India during the peak phase, while negative (positive) anomalies cover the sub-Himalayan region and southeast India. During the final stage of the active (break) period, the positive (negative) rainfall anomalies move toward the foothills of the Himalayas while peninsular India is covered with opposite sign anomalies. The number of days on which lows and depressions are present in the region during active and break periods is consistent with the rainfall analysis. The number of depressions during the active phase is about 7 times that during the break phase.

Using multichannel singular spectrum analysis of the daily rainfall anomalies, the seasonal monsoon rainfall is found to consist of two dominant intraseasonal oscillations with periods of 45 and 20 days and three seasonally persisting components. The 45- and 20-day oscillations are manifestations of the active and break periods but contribute very little to the seasonal mean rainfall. The seasonally persisting components with anomalies of the same sign, and covering all of India, have a very high interannual correlation with the total seasonal mean rainfall. These results support a conceptual model of the interannual variability of the monsoon rainfall consisting of seasonal mean components and a statistical average of the intraseasonal variations. The success in the prediction of seasonal mean rainfall depends on the relative strengths of the seasonally persisting components and intraseasonal oscillations.

1. Introduction

The intraseasonal variation of the Indian monsoon consists of “active” periods of high rainfall and “break” periods of deficient or no rainfall during the summer season [June–September (JJAS)]. The JJAS seasonal mean rainfall varies from year to year and is known to have strong associations with other global phenomena through the influence of sea surface temperature (SST), snow, and soil moisture (see, e.g., Krishnamurthy and Kinter 2003). Based on model experiments, Charney and Shukla (1981) suggested that a large part of the seasonal mean monsoon variability is related to the slowly varying boundary conditions such as the SST and albedo and therefore potentially predictable on a longer time scale. By analyzing 70-yr-long high-resolution data of observed daily rainfall over India, Krishnamurthy and Shukla (2000) suggested a conceptual model of the interannual variability of the Indian monsoon to consist of a linear combination of a largescale persistent seasonal mean component and a statistical average of the intraseasonal variations.

The conceptual model put forward by Krishnamurthy and Shukla (2000) recognized that in addition to a seasonally persisting component, related to the boundary conditions, there are other significant intraseasonal components, and it was based on the following results of their study. The dominant mode of the daily rainfall has anomalies of one sign over central India and anomalies of opposite sign over the foothills of the Himalayas in the north and over southeast India. The dominant pattern of the seasonal rainfall anomalies, however, has a large-scale spatial pattern with anomalies of the same sign over all of India and persists throughout the monsoon season. Once the seasonal mean anomalies are removed, the nature of the intr-
traseasonal variability of the daily rainfall anomalies is not different from one year to another, and more importantly between drought years and flood years. However, the major drought (flood) years are characterized by the presence of a strong seasonal signature of negative (positive) rainfall anomalies covering all of India for the entire monsoon season. The large-scale seasonally persistent pattern can be part of the low-frequency components of the monsoon system influenced by the slowly varying land and ocean boundary anomalies. These results and the conceptual model imply that the success in predicting the seasonal mean rainfall over India depends on the relative magnitudes of the intraseasonal component and the seasonally persisting component.

The intraseasonal variation of the Indian monsoon is known to consist of fluctuations on two time scales broadly falling in the range of 10–20 and 30–60 days. However, the time scale indicated by individual studies has varying ranges such as 10–80, 10–20, 30–60, 40–50 days, etc. The 10–20-day variability was observed in the spectra of pressure, cloud cover, rainfall, and static stability over the Indian monsoon region by Krishnamurti and Bhalme (1976) and in cloudiness data by Yasunari (1979). These results were based on data covering one to three monsoon seasons. A spectral peak in the 40–50-day range was found in a long record of daily rainfall over India by Hartmann and Michelsen (1989) while several studies (e.g., Yasunari 1979; Lau and Chan 1986) have noted the variability on the same time scale in convection data over a larger monsoon region. The presence of 10–20- and 30–60-day variability was also found in a principal oscillation pattern analysis of outgoing longwave radiation (OLR) and reanalysis circulation products for 1979–95 by Annamalai and Slingo (2001). They estimated that 10–20- and 30–60-day fluctuations explain about 25% and 66%, respectively, of the total intraseasonal variability. However, Goswami et al. (1998), who also found the intraseasonal modes on the same two scales in the reanalysis circulation data, estimated that the two modes explain about 10%–25% of the total daily variance.

Most studies associate the intraseasonal variations on the two dominant time scales with the active and break phases of the monsoon. Although rainfall is the most important manifestation of the monsoon variability and the most direct cause of the socioeconomic impact of monsoon that is often cited, there has been no study showing a direct correspondence between the active and break periods observed in the rainfall and the intraseasonal modes noted in other monsoon variables. The presence of the 10–20- and 30–60-day variability in a long record of the daily rainfall over India has also not been shown previously.

The aforementioned results of Krishnamurthy and Shukla (2000) suggest that the prediction of the seasonal mean monsoon rainfall over specific regions depends on the relative strengths of the 10–20- and 30–60-day fluctuations and the component with the seasonal signature that is presumably influenced by boundary forcing. An alternate interpretation of the Charney–Shukla hypothesis as to what determines the seasonal mean rainfall suggests that the boundary conditions merely alter the probability distribution function (PDF) of the rainfall to have a bias toward the active or break phase (Palmer 1994). In this scenario, the seasonal mean rainfall is determined by a bimodal PDF of rainfall and depends on the frequency and length of active and break phases. Goswami and Ajaya Mohan (2001) identified a mode of variability in the reanalysis winds at 850 hPa as common to both intraseasonal and interannual time scales and presented an asymmetric bimodal PDF of the intraseasonal mode. They related the bimodality of the PDF to active and break periods defined on the basis of an index of 850-hPa zonal winds over the Bay of Bengal. In an empirical orthogonal function (EOF) analysis of the reanalysis winds at 850 hPa, Sperber et al. (2000) identified the third EOF of the daily winds and the fourth EOF of the seasonal winds as a common mode of intraseasonal and interannual variability, but found no bimodality in the PDF of the principal component (PC) of the intraseasonal mode. Lawrence and Webster (2001) found that the intraseasonal variability of OLR for the period 1975–97 was moderately correlated with the seasonal mean Indian rainfall but was uncorrelated with the seasonal SST anomalies. Singh et al. (1992) found that the intraseasonal variability of the rainfall over India was not related to either the total seasonal rainfall or the El Niño–Southern Oscillation (ENSO).

The above discussion points to an obvious need for clarification of the relation between the intraseasonal variability and the seasonal mean monsoon rainfall over India. The purpose of this paper is to identify the modes of intraseasonal variability in terms of oscillatory components and components with seasonal signature in the monsoon rainfall. The relation between the intraseasonal components and the JJAS seasonal mean rainfall will be investigated. The space–time structure of the active and break phases of the monsoon will be examined and the correspondence to intraseasonal modes of variability on two dominant time scales will be established. An important aspect of this study is that the results are based on the analysis of a long record of high-resolution daily rainfall over India rather than us-
ing reanalysis winds or OLR. The results of this paper will strongly support the conceptual model suggested by Krishnamurthy and Shukla (2000) and show that the intraseasonal modes on two different time scales (20 and 45 days) oscillate about seasonally persisting components that are shown to be the main contributors to the seasonal mean rainfall.

The data and methods of analysis used in this study are described in section 2. The life cycles of the active and break periods of the monsoon rainfall are discussed in section 3. Section 4 presents an analysis resolving the daily rainfall over India into two dominant oscillatory modes and seasonally persisting components. The relation between these components and the seasonal mean rainfall is discussed. Conclusions are provided in section 5.

2. Data and methods

a. Data

The intraseasonal variability of the monsoon is studied in this paper by analyzing gridded daily rainfall data for the period 1901–70. The data originated from observations made by the India Meteorological Department (IMD) at more than 3700 rain gauge stations in India and were later transformed to a 1° latitude × 1° longitude grid over India by Hartmann and Michelsen (1989). Each grid box in this dataset has observations from several stations for most of the time period. This dataset was earlier used by Krishnamurthy and Shukla (2000), who filled missing data points for some of the days by linear interpolation.

Over India and the adjoining Indian Ocean region, the main rain-producing systems are the monsoon trough that moves north–south and the transitory low pressure systems (LPSs). The LPSs are categorized as lows, depressions, cyclonic storms, severe cyclonic storms, and hurricanes based on their intensity. The lows (systems with wind speeds up to $9 \text{ m s}^{-1}$) and the depressions (winds in the range $9–17 \text{ m s}^{-1}$) are major contributors to the monsoon rainfall. Most of the LPSs are formed east of $80^\circ\text{E}$ over the Bay of Bengal and move in a northwest direction across central and north India; only a few systems are formed over the Arabian Sea. This study has examined the LPS data consisting of daily location and intensity during the life of each LPS from the compilation of Mooley and Shukla (1987) who followed an objective criterion based on the central pressure to classify the LPSs for the period 1888–1983.

The daily rainfall climatology was calculated as the 70-yr mean of the total daily rainfall for each calendar day of the year and was subtracted from the total daily rainfall to obtain the daily rainfall anomaly. The JJAS seasonal rainfall anomaly was computed by averaging the daily values over 1 June to 30 September. The daily rainfall data were converted to 5-day running means to obtain a more coherent analysis without the very high frequency fluctuations.

b. Multichannel singular spectrum analysis

The dominant spatial patterns of the daily and seasonal monsoon rainfall were earlier found by an EOF analysis of the JJAS rainfall anomalies (Krishnamurthy and Shukla 2000). To identify the temporal variability and to determine the coherent intraseasonal space–time patterns of the rainfall, the method of analysis used in this study is the multichannel singular spectrum analysis (MSSA). This data-adaptive method was applied to study the intraseasonal variability in the midlatitudes by Plaut and Vautard (1994) and was reviewed by Ghil et al. (2002) who discuss the method’s applicability to climate variability on different time scales. Both these papers provide the mathematical formulation and technical details of MSSA and point out its equivalence to extended EOF (EEOF) analysis. The following brief description of MSSA is based on the discussion of the method by Plaut and Vautard (1994) and Ghil et al. (2002).

EEOF analysis and MSSA are both extensions of the familiar EOF analysis but include temporal lags of spatial data to obtain space–time patterns of variability. The temporal and spectral information obtained by the analysis depends on the length of the time lags. While EEOF analysis includes only a few time lags, MSSA typically includes larger number of lags, sufficient to identify oscillations and trends on the time scale of interest and to extract their temporal and spatial properties. MSSA is applied to a dataset consisting of time series of $L$ channels (e.g., points on a grid) given at $N$ discrete times at equally spaced time interval $\Delta t$. The analysis involves constructing a covariance matrix of the multichannel time series at temporal lags ranging from 0 to $M - 1$ and diagonalizing the lag-covariance matrix to yield $LM$ eigenvalues and $LM$ eigenvectors (not necessarily distinct). Alternately, the multichannel time series matrix is augmented with $M$ lagged copies of itself, and a singular value decomposition of the augmented matrix is carried out. The parameter $M$ is called the window length. The eigenvectors are the space–time EOFs (ST-EOFs), each an $M$ sequence of maps, describing space–time patterns of decreasing importance as the corresponding eigenvalues decrease. The projection coefficients of the data onto the ST-EOFs are the space–time principal components (ST-PCs) of time length $N' = N - M + 1$, and the variance is given by the eigenvalues.
An oscillation in the time series is identifiable when two consecutive ST-PCs with nearly equal eigenvalues are in phase quadrature. The corresponding ST-EOFs in this case are also nearly periodic with the same period and in phase quadrature. The period and spatial pattern of such a nonlinear oscillation are same as those of the ST-EOFs. It is possible to distinguish oscillations possessing the same spatial patterns but different periods as well as oscillations with same period but with orthogonal spatial patterns. The eigenmodes not associated with oscillatory pairs also provide useful information, particularly about trends and persisting patterns.

The part of the original time series corresponding to a particular eigenmode can be extracted as space–time reconstructed components (RCs) defined by Plaut and Vautard (1994). The RCs are simply projections of the data onto the corresponding $M$ ST-EOFs and are multichannel (or spatial grid) maps whose time length and sequence are exactly those of the original time series. The sum of all the RCs reproduces the original time series. For an oscillation represented by a pair of eigenmodes, the RC is sum of the individual RCs of the pair. The amplitude $A(t)$ and the phase angle $\theta(t)$ of the oscillation can be determined from the RC using the method provided by Moron et al. (1998). The phase angle $\theta$ varies from 0 to $2\pi$ for each cycle of the oscillation. The periods of the oscillations resolved by MSSA depend on the choice of the window length $M$ and are estimated to be in the range $(M/5, M)$ (Plaut and Vautard 1994).

c. Space–time frequency spectrum

To investigate whether the rainfall anomaly has components that are propagating, space–time spectral analysis is used. This technique has been used in intraseasonal studies (e.g., Wheeler and Kiladis 1999) to identify the spatial scales and associated characteristics with different frequencies of variability in the data. The space–time domains of the total rainfall anomalies and the RCs from MSSA are converted into wavenumber–frequency domains. This study applies the spectral analysis to data in a domain limited to India to look for propagating waves in north–south and east–west directions as well as standing patterns. The spectra are computed by performing fast Fourier transform of the discrete data in space and time. Because of the limited domain of the data, the gravest mode (wavenumber 1) of this analysis corresponds to the meridional and zonal extent of the data. Pratt (1976) has provided helpful discussion to infer propagation properties from space–time spectra.

3. Life cycles of active and break periods

The definition of the active and break periods of the Indian monsoon used in this study is based on the daily rainfall anomalies. A widely used measure of the Indian monsoon is the area averaged rainfall over India (land region); such an average of rainfall anomalies will be referred to as the Indian monsoon rainfall (IMR) index. The active (break) period is identified as the period when the daily anomaly IMR index is above (below) a certain positive (negative) threshold for at least five consecutive days, the threshold being one-half of the standard deviation of the IMR index. Krishnamurthy and Shukla (2000) showed that the IMR index has very good daily correlation with the principal component of the most dominant mode of the daily rainfall over India that provides a dynamically consistent description of the active and break phases. For JJAS 1901–70, this criterion yields 214 active periods and 196 break periods with the longest active and break periods extending to 29 in 1902 and 42 days in 1918, respectively. Since the active and break phases have convective–dynamic origin, it is also possible to define them using indices based on dynamical variables (see, e.g., Webster et al. 1998; Goswami and Ajaya Mohan 2001; Goswami et al. 2003). However, because of the propagating nature of the intraseasonal variations, the local active and break phases occur at different times in different locations over the larger Indian monsoon region. For example, in the study of Goswami et al. (2003), the active minus break composite based on a dynamical index defined mainly over the Bay of Bengal shows maximum rainfall over the Bay of Bengal and far less intense rainfall over Indian land points (see their Fig. 2).

a. Evolution of active and break periods

Lagged composites of daily rainfall anomalies with respect to the midpoints of the active and break periods were constructed to study the evolution of the spatial structure of the rainfall during the lives of the active and break phases. The lagged active composites for lags ranging from −12 to +10 days at intervals of two days are shown in Fig. 1 where lag 0 refers to the midpoint of each active period (of varying length) during JJAS 1901–70. On average, the active period lasts for about 16 days starting with positive rainfall anomalies appearing in the Western Ghats while northern India is covered with weak negative rainfall anomalies (lag −8). At lag −6, the rainfall over the Western Ghats intensifies and positive anomalies appear over the east coast while most of India north of about 22°N is covered with weak negative anomalies. During the next four days (lags −4 and −2 composites), the region of positive anomalies

Given the context and nature of the text, it seems like this extract is discussing methods and results related to the analysis of rainfall anomalies in the Indian monsoon. The text outlines the identification of oscillations in the time series, details on reconstructing components, and the definition of active and break periods for the monsoon system. It also mentions the lagged composites to show the evolution of rainfall patterns during active and break phases.

It is crucial to note that the text includes technical terms and methods specific to climate science, such as spectral analysis, space–time reconstructions, and intraseasonal variability. The provided extract is a part of a larger scientific paper or report, and the full context would likely include more detailed figures, tables, and empirical data analysis.
expands over central India with increased intensity of rainfall and negative anomalies are established over southeast India and the sub-Himalayan region in the north. At the peak of the active period (lag 0 composite), all of central India and the Western Ghats are covered with strong positive rainfall anomalies, and the negative anomalies near the foothills of the Himalayas have also intensified. Over the next four days (lags +2 and +4 composites), the rainfall weakens over the Western Ghats and the eastern part of central India while the maximum rainfall occurs over the western part of central India accompanied by slightly increased rainfall over north India. During the subsequent four days (lags +6 and +8 composites), the positive rainfall anomalies weaken and move northward and closer to the foothills of the Himalayas while the peninsular region (south of about 20°N) is covered with weak negative rainfall anomalies. The lagged break composites (figure not shown) look very much similar to the active composites in Fig. 1 but with rainfall anomalies of opposite sign.

b. Composites of low pressure systems

The composites of LPS-days for all active and break periods during JJAS 1901–70 were constructed. An LPS-day is defined as one day on which an LPS (low, depression, etc.) exists in the Indian monsoon region. In particular, depression-day refers to one day on which a depression (category 2 LPS) is observed, and the active and break composites for depression-days are
shown in Figs. 2a and 2b, respectively. The mean life of the depression formed over the Bay of Bengal is 5 days, whereas it is 3 days for those formed over land and over the Arabian Sea (Mooley and Shukla 1987). Therefore, a single depression is represented by several depression-days (equal to its life) in the composites following its evolution. The composites in Figs. 2a and 2b show the locations of all the depression-days during active and break periods, respectively. There are 679 depression-days in the active composite (Fig. 2a) and 105 depression-days in the break composite (Fig. 2b), showing clearly that most depression-days during the monsoon season are associated with the active periods.

Most of the depression-days in the active period (Fig. 2a) are located in the region of maximum rainfall (Fig. 1) and extend across the entire central India. The maps containing the trajectories of all the depressions during this period provided by Mooley and Shukla (1987) show that the active composite in Fig. 2a is associated with depressions formed mostly over the Bay of Bengal

---

**Fig. 2.** (a) Active phase composite (red dots) and (b) break phase composite (blue dots) of depression-days. Each dot represents the location of the depression for a day (or depression-day). The composites were constructed for all active and break days during JJAS 1901–70. (c) Lagged active phase composites (red) and lagged break phase composites (blue) of depression-days for the period JJAS 1901–70. Lag 0 corresponds to the midpoint of each active or break phase.
and over land and moving in west-northwest direction parallel to the axis of the monsoon trough. Such movement of the depressions is consistent with the northwest-southeast tilt in the peak rainfall bands of the active composite (Fig. 1). A remarkable difference between Figs. 2a and 2b is the location of the depressions. During the break phase, the locations of the depressions are clearly toward the northern edge of the locations during the active phase. The depression-days of the break composite occur when the monsoon trough has moved toward the foothills of the Himalayas. The composites of low-days (i.e., the days on which lows were present) were also examined (figure not shown) and found to consist of 723 and 345 low-days for the active and break periods, respectively, and show spatial structures similar to the composites of the depression-days shown in Figs. 2a and 2b. Similar composites of LPS were shown by Goswami et al. (2003) based on their definition of active and break phases over the Bay of Bengal for the period 1954–83.

The lagged active and break composites of the total number of depression-days during 1901–70 are shown in Fig. 2c. These composites are plotted at one-day interval for lags ranging from −22 to +22 days with reference to the midpoint of the active or break period as lag 0. The total number of depression-days reaches a peak value of about 88 during the active phase whereas it goes down to about 2 during the peak of the break phase. The lagged composites of the depression-days are consistent with the life cycles of the rainfall anomaly composites shown in Fig. 1.

c. Area-averaged rainfall and relation to seasonal rainfall

The lagged active and break composites of daily anomaly IMR index for JJAS 1901–70 were constructed to show that the active and break phases can be considered as fluctuations about a mean value of the JJAS seasonal rainfall. The lagged active composites of the IMR index constructed separately for strong and weak monsoon years are shown in Fig. 3. The eight strong and eight weak monsoon years selected for this purpose are exactly the same as those defined by Krishnamurthy and Shukla (2000), and the JJAS seasonal rainfall anomalies averaged over strong and weak years separately are also plotted in Fig. 3. The composites in Fig. 3 show that while the active phases fluctuate about the average JJAS seasonal anomaly of 1.07 mm day$^{-1}$ during strong monsoon years they fluctuate about the average of −1.22 mm day$^{-1}$ during weak monsoon years. For the entire life cycle of the active phase, strong monsoon years have a persistent rainfall anomaly of about 2 mm day$^{-1}$ higher compared to weak monsoon years.

![Fig. 3. Lagged active phase composites of the IMR index (mm day$^{-1}$) during strong monsoon years (red) and weak monsoon years (blue) for the period 1901–70. Lag 0 corresponds to the midpoint of each active or break phase. The solid (dashed) green lines represent the JJAS seasonal mean IMR index averaged over strong (weak) monsoon years.](image)

Similar behavior was also seen in the break composites (figure not shown). This result supports the conceptual model of Krishnamurthy and Shukla (2000), which suggests that the active and break phases are fluctuations about seasonally persisting components that vary on interannual time scale.

4. MSSA of rainfall anomalies

To resolve the oscillations and persisting signals present in the monsoon variability, MSSA was applied to daily Indian rainfall anomalies for the period 1901–70 following the method detailed by Plaut and Vautard (1994) and Moron et al. (1998). Similar to the EOF analysis of the same data for JJAS months (equivalent to MSSA with $M = 1$) by Krishnamurthy and Shukla (2000), MSSA was carried out using daily rainfall anomalies for 122 days of JJAS of each year with a lag window length $M = 61$ days. With these specifications and ensuring that no discontinuous data enter into the lagged data during JJAS of each year, each ST-PC is 62 days long each year and each ST-EOF consists of maps in a sequence of 61 lags. The space–time RC of each eigenmode was computed for all 122 days of JJAS of each year corresponding to the exact sequence of the original time series. According to the estimate of Plaut and Vautard (1994), the analysis of this study can expect to distinguish oscillations with periods in the range of 12 to 61 days. The analysis was repeated with $M = 51$ and 71 days (using data longer than JJAS for latter case) and the results were found to be similar to those with a 61-day window. Consistent results were also obtained with the data filtered by retaining the first 10
modes of a spatial EOF analysis. This paper will discuss the analysis of full data with $M = 61$ days.

a. Eigenmodes

The eigenvalue spectrum from the MSSA of daily rainfall anomalies is shown in Fig. 4a with the first 30 eigenvalues plotted as percentage fractions of the total variance. It appears that the eigenvalues of order 9 onward are close to reaching the noise level. The first seven eigenmodes were found to be most relevant to describe the dominant modes of the intraseasonal variability of the monsoon rainfall, and explain about 22.2% of the total variance. The eigenmode pairs with almost equal eigenvalues are 1–2, 3–4, and 6–7 as seen in Fig. 5a. However, using the criteria for identifying two consecutive eigenmodes to form an oscillatory pair as specified by Plaut and Vautard (1994) (also see section 2), it is found that pairs 1–2 and 6–7 are oscillatory whereas the pair 3–4 is not. Therefore, eigenmodes of order 3, 4, and 5 emerge as nonoscillatory. Using the ST-EOFs and ST-PCs, the RCs for the first seven modes were computed. The RC of mode $i$ will be denoted as $R(i)$ and $R(i) + R(j)$ as $R(i,j)$.

b. 45- and 20-day oscillations

The reconstructed oscillations 1–2 and 6–7 (oscillatory parts of the total rainfall anomaly) are the sums $R(1,2)$ and $R(6,7)$, respectively. The phase angle and the amplitude of the oscillatory pairs 1–2 and 6–7 were determined. The approximate power spectra of all-India average of $R(1,2)$ and $R(6,7)$ are shown in Fig. 4b. The pair 1–2 has a broad spectrum centered at 45 days whereas the spectrum of pair 6–7 is centered at 20 days. These are well-defined broad spectra compared to the continuous spectrum of the total daily rainfall anomaly shown in Fig. 4b for comparison. The modes 3, 4, and 5, however, have most of the power in their spectra toward the red part indicating that the components are trends or persisting signals although weak variability associated with peaks close to 30 days are also visible (spectra not shown). The wavenumber–frequency spectra of these modes will be discussed later to get a more accurate understanding of the spectral properties.

The daily phase angle $\theta$ of the two oscillations and the corresponding RCs at a particular channel (grid
Fig. 6. (a) Phase composites of $R(1, 2)$ of the oscillation 1–2 with a period of about 45 days and (b) phase composites of $R(6, 7)$ of the oscillation 6–7 with a period of about 20 days. Units are in mm day$^{-1}$. The phase number is given at the top left corner of each panel.
point at 77°E and 20°N) for JJAS 1952 and 1955 (randomly selected channel and years as examples) are shown in Fig. 5 along with the IMR index of the daily total rainfall anomaly. The oscillations $R(1, 2)$ and $R(6, 7)$ capture the variations in the daily rainfall at, respectively, 45- and 20-day time scales. The difference in the fraction of total variance explained by $R(1, 2)$ (10.1%) and $R(6, 7)$ (3.7%) is also evident in the amplitudes of the RCs plotted in Fig. 5. The 1–2 and 6–7 modes are nonlinear oscillations showing anharmonic shapes, as evident in Fig. 5. These oscillations are modulated in amplitude, phase, and frequency. The variations in the amplitude and phase of the oscillations are reflected in the broadness of the spectra shown in Fig. 4b. The RCs of the two nonlinear oscillations vary in a nonperiodic manner (Fig. 5). It is well known that chaotic variations of a nonlinear system consist of unstable periodic orbits. During its evolution, the system comes close to such periodic orbits from time to time and may linger around them for a while. The oscillatory pairs of MSSA capture such “ghost” limit cycles (see Ghil et al. 2002 for more details). The origin of such unstable periodic orbit may be related to some fundamental dynamical instability of the system.

The space–time structure of the 45- and 20-day oscillations can be visualized by constructing composites of $R(1, 2)$ and $R(6, 7)$ based on the phase angle $\theta$ of the respective oscillation. The interval $(0, 2\pi)$ in which $\theta$ varies is divided into eight equally spaced intervals such that $(k - 1)\pi/4 \leq \theta(t) < k\pi/4$ with $k = 1, \ldots, 8$. The
phase $k$ composite is constructed by averaging the RC over all instances of the oscillation in phase $k$. The phase composites were constructed separately for the two oscillations.

The composites of $R(1, 2)$ for the phases of the oscillatory pair 1–2 shown in Fig. 6a reveal an average oscillatory cycle consisting of active and break phases with an average period of about 45 days. Each phase lasts about 5–6 days. The phase 1 composite shows the developing stage of the active period with positive rainfall anomalies over most of the peninsular region with maximum values over the Western Ghats. The active phase gets established and peaks in phase 2 and 3 composites with strong positive rainfall anomalies over central India and the Western Ghats and negative anomalies near the foothills of the Himalayas and over southeast India. The final stage of the active phase with positive rainfall anomalies weakening and moving closer to the foothills of the Himalayas is seen in the phase 4 composite. Similar onset, establishment, and the final stages of the break period are seen in phase 5–8 composites, which are almost exactly the opposite of phase 1–4 composites, respectively. The space–time structure of the active phase of this 45-day oscillation follows a sequence similar to the life cycle of the active phase shown in Fig. 1 using composites based on active days defined by actual rainfall anomalies. The only difference lies in the period of the cycle between the two composites.

The phase composites of $R(6, 7)$ for the phases of the oscillatory pair 6–7 are shown in Fig. 6b. The 6–7 oscillation also consists of a cycle of active and break phases similar to that of the 1–2 oscillation (shown in Fig. 6a) except that the average period is about 20 days and the amplitude is about half that of the 1–2 oscillation.

Similar phase composites of the number of depression-days also confirm the space–time structure of the 45- and 20-day oscillations. There are 557 depression-days during phases 2 and 3 of the active phase of covering central India and part of the Bay of Bengal (Fig. 7a) while there are only 182 depression-days during phases 6 and 7 of the break period (Fig. 7b) in the 1–2 oscillation. Similar composites of the 6–7 oscillation show 472 depression-days during the active phase (Fig. 7c) and 262 depression-days during the break phase (Fig. 7d). The phase composites in Fig. 7 have good resemblance to the active and break composites of the depression-days based on the total rainfall anomalies shown in Fig. 2.

The phase composites were also constructed using a shorter phase interval of $\pi/12$ to examine the evolution of the oscillation on a finer time scale. The phase composites of the total rainfall anomalies were also examined for the two oscillations and were found to possess spatial structure similar to and magnitudes comparable to the composites of the corresponding RC. For a compact display of one complete phase cycle of each oscillation, the area averages of the phase composites of $R(1, 2)$ and $R(6, 7)$ over India (similar to the IMR index) are plotted in Fig. 8a. While the average cycles of both $R(1, 2)$ and $R(6, 7)$ consist of well-defined active and break phases, the peak amplitudes of $R(1, 2)$ and $R(6, 7)$ are about 1.2 and 0.6 mm day$^{-1}$, respectively. The amplitude of $R(1, 2)$ attains its peak value at phase $\pm \pi/2$ whereas it happens at $\pm 2\pi/3$ for $R(6, 7)$. The phase composites of the depression-days (Fig. 8b) show depression activities consistent with the composites of RCs (Fig. 8a) with most of the depression-days occurring during the active period. The phase composites of the total rainfall anomaly for the two oscillations (Fig. 8c) are very close to those of the RCs (Fig. 8a) confirming that the two oscillations represent the dominant modes of intraseasonal variability. Comparing with the composites in Fig. 1, it is evident that $R(1, 2)$ and $R(6,$
7) together contribute considerably to the amplitude of the total rainfall anomaly during active and break periods. The combination of $R(1, 2)$ and $R(6, 7)$ plays a dominant role in determining the phase and length of the active and break periods represented in Fig. 1. The actual contribution of these two oscillatory modes to the total rainfall anomalies during the monsoon season will be discussed next.

c. Seasonally persisting components

The seasonal mean properties of the first seven eigenmodes of the MSSA will now be discussed to reveal the relative roles of these modes in determining the seasonal mean rainfall. It is necessary to first find the relative contributions of the seven modes to the daily total rainfall anomalies during the active and break phases. For the kind of analysis performed in this study, the nonoscillatory modes 3, 4, and 5 do not show much difference among themselves. The distinction may lie in what factors (e.g., external forcing) are responsible for producing these components. Therefore, further discussion will consider the RCs of the modes 3, 4, and 5 together and will focus on the sum $R(3) + R(4) + R(5)$, denoted as $R(3, 4, 5)$. Similar to the composites of the total rainfall anomalies shown in Fig. 1,
the active and break composites of daily $R(1, 2)$, $R(3, 4, 5)$, and $R(6, 7)$ were constructed using the criterion for active and break periods specified in section 3. The difference between the active and break composites of the RCs and the total rainfall anomaly are shown in Fig. 9a. The daily composites of the components shown have spatial structure similar to that of the total anomaly but with different magnitudes. The component $R(1, 2)$ has about twice the magnitude of $R(6, 7)$, but the two oscillations together contribute more than $R(3, 4, 5)$ to the total rainfall anomaly.

To investigate if any of the eigenmodes contain seasonal signature and to determine if the oscillatory modes 1–2 and 6–7 fluctuate about a seasonal signal, JJAS seasonal means of the RCs were computed. The strong and weak monsoon year composites of the JJAS seasonal mean $R(1, 2)$, $R(3, 4, 5)$, and $R(6, 7)$ were constructed using the same compositing years used in section 3c. The difference between strong and weak composites of the RCs and the total seasonal rainfall anomaly are presented in Fig. 9b. The seasonal means of $R(1, 2)$ and $R(6, 7)$ are negligible (note the scale of each composite) although $R(6, 7)$ has at least the same sign and somewhat similar spatial structure as those of the total anomaly. On the other hand, $R(3, 4, 5)$ has close spatial resemblance to the total anomaly with comparable magnitude. The daily and seasonal composites in Fig. 9b strongly indicate that the 45- and 20-day oscillations fluctuate about a seasonally persisting signal represented by $R(3, 4, 5)$.

To quantify the seasonal behavior of the components for the entire period of 1901–70, the area averages of the JJAS seasonal means of $R(1, 2)$, $R(3, 4, 5)$, and $R(6, 7)$ over India (like IMR index) were computed. The time series of the RCs are shown in Fig. 10 along with that of the total rainfall anomaly (seasonal IMR index). The seasonal means of $R(1, 2)$ and $R(6, 7)$ are very small for the entire period. While $R(1, 2)$ has insignificant negative correlation ($-0.14$) with the total anomaly, $R(6, 7)$ has a small positive correlation (0.36). However, $R(3, 4, 5)$ has the same magnitude as that of the total rainfall anomaly, and the correlation between them is also very high (0.83).

The daily variation of the oscillatory modes and the seasonally persisting components were examined for all years. Two particular years that will be discussed will serve as good examples of the behavior of the components found in the detailed examination. The selected years are the weak monsoon of 1918 and the strong monsoon of 1959 for which the JJAS seasonal means of $R(1, 2)$, $R(3, 4, 5)$, $R(6, 7)$, and the total rainfall anomaly are plotted in Fig. 11. The total anomaly is strongly negative (positive) over most of India west of $85^\circ$E for 1918 (1959). These structures are also present in the maps of $R(3, 4, 5)$ with comparable magnitude. However, $R(1, 2)$ and $R(6, 7)$ have magnitudes an order less compared to the total seasonal anomaly and bear no spatial resemblance to the total anomaly.

The daily variations for 1918 and 1959 are shown with the area averages of the same components over India in Fig. 12. For most of the season, the total anomaly and $R(3, 4, 5)$ vary nonperiodically with strong negative (positive) anomalies during 1918 (1959). However, both $R(1, 2)$ and $R(6, 7)$ show nonperiodic fluctuation on the time scales of their respective periods of variability without any bias toward positive (strong monsoon) or negative (weak monsoon) sign. Clearly, $R(3, 4, 5)$ possesses a persisting seasonal signature that characterizes the weak and strong years. During 1959, $R(3, 4, 5)$ also shows a mixed variation on the time scale of about 30 days. However, the MSSA did not resolve an oscillation on the 30-day time scale.

\textbf{d. Propagation}

The propagation characteristics of the components may be seen from the frequency–wavenumber spectra.
shown in Fig. 13. The meridional spectra were calculated for $R(1, 2)$, $R(3, 4, 5)$, and $R(6, 7)$ averaged between 68° and 96°E over the latitude domain 8°–32°N to provide information about north–south propagation. For east–west propagation, the RCs were averaged between 8° and 32°N and the spectra were obtained for the longitude domain 68°–96°E. The spectra were computed for each year separately and then averaged over the period 1901–70.

The broad spectra of $R(1, 2)$ in Figs. 13a and 13b indicate that oscillation 1–2 shows northward as well as eastward propagation with a 45-day period. However, the oscillation 6–7 is a propagating wave in the northward and westward direction with a period of 20 days as inferred from the broad spectra of $R(6, 7)$ in Figs. 13c and 13d. In Fig. 13, wavenumber 1 corresponds to the domains 8°–32°N and 68°–96°E, respectively, for the meridional and zonal spectra. The 45-day oscillation reflects the movement of the monsoon trough in the southwest–northeast direction whereas the 20-day oscillation represents the westward movement of the LPS such as lows and depressions while embedded in the monsoon trough.

The redness in the spectra of $R(3, 4, 5)$ in both Figs. 13e and 13f indicates that a standing pattern covering all of India with either positive or negative rainfall anomaly persists throughout the season. However, the spectra also exhibit a weaker component that varies on

Fig. 11. JJAS seasonal means of total rainfall anomaly and RCs for (a) weak monsoon year 1918 and (b) strong monsoon year 1959. Units are in mm day$^{-1}$. The components plotted are identified at the top right corner.
30-day time scale possibly as a combination of stationary mode and a northeast-propagating mode with the same sign of anomaly over all of India.

5. Summary and conclusions

By analyzing 70-yr-long observed daily rainfall data over India, this study has found that rainfall over India during the monsoon season consists of intraseasonal oscillations on different time scales fluctuating about seasonally persisting components. It was also found that the life cycle of the active (break) period of the monsoon lasts about 16 days on average and starts with positive (negative) rainfall anomalies over the Western Ghats and eastern part of central India. The positive (negative) rainfall anomalies intensify and cover all of central India and parts of north India while negative (positive) anomalies are established over the sub-Himalayan region and over southeast India during the subsequent evolution of the active (break) period. After the peak phase, the rainfall anomalies move northeast toward the foothills of the Himalayas with diminished intensity while anomalies of opposite sign develop over the entire peninsular region. The lagged composites of the averaged rainfall anomalies for strong and weak monsoon years showed that the active and break phases for any year fluctuate about the seasonally persistent mean anomaly for that year. The number of days when low pressure depressions exist was found to be about 7 times more during the active period than during the break period and showed consistent variation with the rainfall anomalies. The dramatic difference in the number and location of the depressions between Figs. 2a and 2b is the basis for an important but yet to be resolved question, whether the active and break phases are caused by the variation in the formation of monsoon depressions or whether the difference in large-scale flows during the active and break periods cause the variation in formation of the depressions.

The MSSA of daily rainfall anomalies showed that the intraseasonal monsoon variability consists of two dominant nonlinear oscillations with broad spectral peaks centered at 45 and 20 days. These oscillations are modulated in amplitude, phase, and frequency and vary in a nonperiodic manner. The oscillatory pairs of MSSA capture the unstable limit cycles embedded in the chaotic variation of the total rainfall anomalies. It was shown that these two nonlinear oscillations together correspond to the life cycles of active and break periods of the monsoon. Each mode goes through an active phase and a break phase during one period of oscillation following the same sequence of spatial structure of active and break periods described in the previous paragraph. The amplitude of the 45-day oscillation is about twice that of the 20-day oscillation. While the 45-day mode exhibits northeast propagation, the 20-day oscillation shows northwest propagation. The oscillations are associated with the number of lows and depressions varying in a manner consistent with active and break periods. The two oscillations play a major role in determining the length and phase of the active and break periods and contribute considerably to the daily rainfall anomalies during those periods.

The 45- and 20-day oscillations, however, make almost no contribution to the seasonal mean rainfall. Three other intraseasonal eigenmodes from MSSA were identified as components with seasonal signature. The seasonal means of these three intraseasonal modes have very high interannual correlation with the seasonal mean of the total rainfall anomaly. The dominant space–time structure of the intraseasonal components with seasonal signature consists of anomalies of the same sign covering almost all of India and persisting throughout the monsoon season, as revealed by MSSA.
and wavenumber–frequency spectra. The seasonally persisting components also include a weak 30-day variation that possibly involves the amplitude variation of a standing pattern that covers India with anomalies of the same sign. The 30-day variation needs further examination by isolating it using some filtering process as MSSA does not resolve it as an oscillatory component.

The results of this study from lag composite analysis and MSSA of daily rainfall provide further support to the conceptual model suggested by Krishnamurthy and Shukla (2000) that seasonal mean monsoon rainfall anomalies consist of a large-scale seasonally persistent component and regional intraseasonal fluctuations. Consistent with the conceptual model, the seasonal rainfall over India is a combination of 45- and 20-day
oscillations fluctuating about large-scale components that persist with same sign throughout the season. It must be noted that only the daily climatology was removed from the data before all the analyses were performed. The conceptual picture was clearly evident in the daily variation of these various components shown for particular years of strong and weak monsoon. The insignificant contributions of the 45- and 20-day oscillations to the seasonal mean rainfall and the presence of a seasonally persisting component further confirm the earlier result of Krishnamurthy and Shukla (2000) that the seasonal mean rainfall is not determined by a bias in the PDF of rainfall toward active or break phase.

The implication of these results for the predictability of the seasonal mean monsoon rainfall is significant. If the intraseasonal modes with seasonal persistence make a relatively large contribution to the seasonal mean rainfall and if they are related to slowly varying boundary forcings or other low-frequency global circulations, the seasonal rainfall anomaly over India may be more predictable. Further work should explore the relation between the boundary forcings, such as SST, soil moisture and snow cover, and the seasonally persisting components (modes 3, 4, and 5) of the rainfall. Further research is also needed to find if higher-order modes and the interaction among different modes can also contribute to the seasonally persisting signal. Although the 20- and 45-day intraseasonal oscillations are found to be small contributors to the seasonal mean rainfall, they are important in determining regional rainfall anomalies. It is also worth investigating what kind of influence the boundary anomalies have on the 45- and 20-day oscillations.

Similar analysis of daily OLR and circulation variables will be helpful to understand the dynamics associated with the intraseasonal modes and the seasonally persisting components of the rainfall. Some studies (e.g., Sikka and Gadgil 1980) have suggested that the active and break periods of the monsoon rainfall over India are associated with the northward propagation of convection zones from the equatorial Indian Ocean to the Indian land region. The analysis of OLR over the monsoon region including the Indian Ocean can help in testing the hypothesis of northward movement of convection. The results of the analysis of OLR and circulation variables over the Indian monsoon region will be presented in another paper.

Acknowledgments. This research was supported by grants from the National Science Foundation (0334910), the National Oceanic and Atmospheric Administration (NA04AR4310034), and the National Aeronautics and Space Administration (NNG04GG46G). The authors thank Rameshan Kallumal for helpful discussions.

REFERENCES


